



# An ECCOMAS Advanced Course on Computational Structural Dynamics

Institute of Thermomechanics Academy of Sciences of the Czech Republic

> Prague Czech Republic

## June 13-17, 2016

Lecturers Prof. K.C. Park University of Colorado, Boulder, USA Prof. Roger Ohayon Conservatoire National des Arts et Métiers, Paris, France Prof. Alain Combescure Institut National des Sciences Appliquées, Lyon, France Prof. Adnan Ibrahimbegovic Université de Technologie Compiègne/ Sorbonne Universités, France Prof. Miloslav Okrouhlík

### Institute of Thermomechanics, Prague, Czech Republic **Dr. Jiří Plešek** Institute of Thermomechanics, Prague, Czech Republic **Prof. Jaroslav Kruis** Czech Technical University in Prague, Czech Republic **Prof. José González** Universidad de Sevilla, Spain **Dr. Anton Tkachuk** University of Stuttgart, Germany **Dr. Radek Kolman** Institute of Thermomechanics, Prague, Czech Republic



## **Topics:**

The course covers topics relating to modern and recent numerical methods in computational structural dynamics, finite element method in linear and nonlinear dynamic cases, wave propagation in solids and its numerical solution, numerical methods in dvnamic crack problems, propagation modern methods for direct time integration and partitioned analysis (domain decomposition methods, FETI, etc..), modal and spectral analysis, coupled problems in mechanics (e.g. fluidstructure interaction), vibroacoustic problems and many others.

The short course is organized under

- European Community on Computational Methods in Applied Sciences
- Central European Association for Computational Mechanics
- Czech Society for Mechanics
- Institute of Thermomechanics, Academy of Sciences of the Czech Republic



## Fee of short course:

Early fee\* (up to March 15, 2016) 400 EUROS - for students and postdocs (confirmation needed) 500 EUROS - for junior and senior researchers 600 EUROS - for industry and private sector Regular fee\* (deadline April 30, 2016) 500 EUROS - for students and postdocs (confirmation needed) 600 EUROS - for junior and senior researchers 700 EUROS - for industry and private sector \*Course fees for ECCOMAS, CEACM and CSM members are reduced by 5%. Short course fees include hard copy of lectures, coffee breaks, social program.

Venue: CTU campus, Prague, Dejvice

WWW: shortcourse2016.it.cas.cz

E-mail: shortcourse2016@it.cas.cz

Contact person: Dr. Radek Kolman (Institute of Thermomechanics, Academy of Sciences of the Czech Republic; <u>kolman@it.cas.cz</u>)

#### **Program of the short course:**

#### Monday

Basics of dynamics

 (M. Okrouhlík)
 Historical background
 Newton's laws
 Newtonian, Lagrangian and Hamiltonian mechanics

 Continuum mechanics I

 (J. Plešek)
 Kinematics of deformations
 Strains and stresses
 Governing equations
 Strong form and boundary conditions

#### 3. Continuum mechanics II

(J. Plešek)

Constitutive equations for small and large deformations Elasticity and plasticity theory Thermodynamics of continuum mechanics

#### 4. Continuum mechanics III

**(R. Ohayon)** Variational formulations in linear dynamics and vibrations Modal analysis Rayleigh quotient, Hamilton's principle

### 5. Dynamics of multibody systems

(A. Ibrahimbegovic) Governing equations Constrains Lagrange equations and Lagrange multipliers Numerical methods in multibody dynamics

#### Tuesday

6. Finite element method I

 (J. González)
 Basics of FEM and discretization
 Weak formulation, stiffness matrix and assembling
 Application of boundary conditions
 Convergence properties of FEM

#### 7. Finite element method II (A. Ibrahimbegovic) Shape functions and higher order FEM Isoparametric formulation Numerical integration Hybrid and mixed formulation, inf-sup condition 8. Finite element method III (A. Tkachuk) Locking phenomena and hourglass effect Assumed strain, enhanced strain FEM, B-bar formulation Reduced integration and stabilization 9. Finite element method IV (J. Kruis) Linear solvers in FEM Matrix factorization Sparse solvers, Krylov methods (especially conjugate gradient method) 10. Finite element method V (A. Ibrahimbegovic) FEM for nonlinear problems Solvers for nonlinear static problems - NR, BGFS, semi-Newton methods, etc. Convergence criteria Wednesday 11. Finite element method VI (J. Kruis) FEM in vibration problems, mass matrix Spectral and modal analysis Numerical methods for eigen-value problem (subspace iteration, etc)

Convergence of FEM in eigen-value problem Dynamic steady state response

## 12. Direct time integration in dynamics I (R. Kolman)

FEM in linear dynamics, formulation of dynamic problems Lumping for mass matrices Introduction into direct time integration basic methods (Newmark method and central difference method) Stability, order and accuracy

(A. Ibrahimbegovic) Dynamic problems Solving of nonlinear time-depend problems 14. Finite element method VII (A. Combescure) Basics of shell theory FEM shell models FEM for shells in dynamics Mass matrices for shells 15. Direct time integration in dynamics II (A. Tkachuk) Time step size estimates – global/local estimate in FEM Treatment of time step size - mass scaling, bi-penalty, etc Application in crash problems

13. Finite element method VI

#### Thuersday

(K.C. Park)

(FETI)

16. Modal reduction and reduction methods in dynamics (R. Ohavon) Variational analysis of dynamic substructuring Substructuring analysis in discretized case Hurty and Craig-Bampton methods 17. Partitioned analysis I (K.C. Park) Theory of Lagrange multipliers Basic theory of partitioned analysis Equations of motion for partitioned systems 18. Dynamic contact problems (A. Tkachuk) FEM in contact problems Penalty method Augmented Lagrangian method Mortar methods 19. Partitioned analysis II

Domain decomposition methods

Coupling of FEM/FEM

Finite element tearing and interconnect

#### 20. Finite element method VII – wave propagation (R. Kolman) Theory of wave propagation in elastic solids Wave speeds in solids Dispersion and frequency analysis of FEM Spurious oscillations and improving of standard methods

#### Friday

21. Modern methods of direct time integration (A. Combescure) Generalized time schemes Asynchronous and variational schemes Sub-cycling methods, coupling of different time schemes 22. Coupled problems -Fluid-structures interactions (K.C. Park) Varionational formulation Methods of discetizations Staggered analysis 23. Boundary element method (J.González) Theory of BEM Numerical aspects of BEM Coupling FEM/BEM 24. Numercial Methods for dynamic crack propagation (A. Combescure) Extended finite element method (XFEM) Meshless methods and Level-set methods Cohesive models in FEM 25. Vibro-acoustic/elasto-acoustic modelling (R. Ohayon) General local equations of vibroacoustic problem Choice of unknown fields and variational formulations of the problem Finite element discretization and reduced order models for the interior problem